Binary Pulsars as Tools to Study Gravity



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By the End You Should Remember...

Binary pulsars

- Excellent tools to test gravity
- Probe a different gravitational field regime
- System diversity = complementarity



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The Binary Pulsar Population

Binary pulsars are "special"

According to the ATNF catalogue:

- 2008 pulsars
- 186 binary pulsars

Binaries:

- Short spin periods
- Old
- Low magnetic fields



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Binary Pulsar Timing and Gravity

Almost textbook examples



Compact objects (point mass)

Precise timing (frequency standard)

Typical TOAs precision is ~0.1% Pspin

 $(t-t_0) + \frac{1}{2}\dot{\nu}(t-t_0)^2 + \dots$



Binary Pulsar Dynamics & Relativistic Effects

Binary Pulsar Timing

Newtonian orbits

Timing binary pulsars allows one to determine 5 Keplerian parameters:

 $P_{\rm h}$

e

ω

- Orbital period
- Eccentricity
- Longitude of periastron
- Projected semimajor axis
- Epoch of periastron

 $x_i \equiv a_i/c \sin i$

 $T_{ heta}$

We measure radial Doppler shifts only... => The orbital inclination angle is unknown.



Arpad Horvath (Wikipedia)

Binary Pulsar Timing

Relativistic orbits

Post-Keplerian (PK) parameters: dynamics beyond Newton.

- PKs are phenomenological corrections (theory-independent).
- PKs are functions of Keplerian parameters, M₁ and M₂.

More than 2 PKs = test of a given relativistic theory of gravity.



Binary Pulsar Timing

Relativistic orbits



Weisberg & Taylor (2005)

- Testing gravity relies on orbital dynamics
- Ideally: pulsar + neutron star
 eccentric + compact orbit
- About 10 known "relativistic" pulsar binaries

PSR B1913+16

First binary pulsar discovered (Hulse & Taylor 1975)

• First indirect evidence of gravitational wave emission (Taylor et al. 1979)

A unique system

The *Double Pulsar* (PSR J0737-3039A/B), is the only known pulsar-pulsar system.

Pulsar A: 23 ms (Burgay et al., 2003) Pulsar B: 2.8 s (Lyne et al., 2004)

Eccentricity: 0.08

Orbital period: 2.4 hrs !!! (v_{orbital} ~ 0.001 c)



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Testing gravity



Kramer et al., 2006

$$\begin{split} \dot{\omega} &= 3T_{\odot}^{2/3} \left(\frac{P_b}{2\pi}\right)^{-5/3} \frac{1}{1-e^2} \left(M_A + M_B\right)^{2/3}, \\ \gamma &= T_{\odot}^{2/3} \left(\frac{P_b}{2\pi}\right)^{1/3} e \frac{M_B (M_A + 2M_B)}{(M_A + M_B)^{4/3}}, \\ \dot{P}_b &= -\frac{192\pi}{5} T_{\odot}^{5/3} \left(\frac{P_b}{2\pi}\right)^{-5/3} \frac{\left(1 + \frac{73}{24}e^2 + \frac{37}{96}e^4\right)}{(1-e^2)^{7/2}} \frac{M_A M_B}{(M_A + M_B)^{1/3}}, \\ r &= T_{\odot} M_B, \\ s &= T_{\odot}^{-1/3} \left(\frac{P_b}{2\pi}\right)^{-2/3} x \frac{(M_A + M_B)^{2/3}}{M_B}, \end{split}$$

Periastron advance

Rate of precession of the periastron: 17°yr⁻¹ !

It takes 21 years to complete a cycle of precession.

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Gravitational redshift and time dilation

Needs to climb to potential well

Clocks tick at variable rate in gravitational potentials

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Gravitational wave emission

Orbit shrinks 7mm/day (coalescence timescale ~ 85 Myrs)

Testing gravity



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Shapiro delay

Light travels in curved space-time

Testing gravity



Kramer et al., 2006

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Testing gravity



Kramer et al., 2006

Mass ratio

Double Pulsar only: mass ratio, R.

 $M_A/M_B = a_B sin(i) / a_A sin(i)$

(theory-independent; at 1PN level at least)

Testing gravity



Kramer et al., 2006

Mass ratio

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Testing gravity



Kramer et al., 2006

Testing GR and gravity

Mass ratio + 5 PK parameters

=> Yields 6-2=4 gravity tests

Best binary pulsar test

Shapiro delay "s" parameter Agrees with GR within 0.05% (Kramer et al. 2006)

Hulse-Taylor pulsar is 0.2%

Relativistic Spin Precession

Spin-orbit coupling induces relativistic spin precession

Precession of the spin angular momentum of a body is expected in relativistic systems.

Parallel transport in a curve space-time changes the orientation of a vector relative to distant observers.

Known as "geodetic precession" or "de Sitter – Fokker precession".



Relativistic Spin Precession

Observational evidence of precession

Changes of pulse shape and polarization over time.

PSR B1913+16 (Kramer 1998, Weisberg & Taylor 2002, Clifton & Weisberg 2008):

Assume the predicted GR rate to map the beam

PSR B1534+12 (Stairs et al. 2004):

• $\Omega_{\rm obs} = 0.44^{+0.48(4.6)}_{-0.16(0.24)} \,^{\circ}/{\rm yr}$

$$\Omega_{\rm GR} = 0.51^{\circ}/{\rm yr}$$



Phenomenology

Pulsar A eclipsed by pulsar B for ~30 seconds at conjunction

Rapid flux changes synchronized with pulsar B's rotation (McLaughlin et al. 2004)



Modeling using synchrotron absorption in a truncated dipole

The "doughnut model" (Lyutikov & Thompson 2006)

Modeling using synchrotron absorption in a truncated dipole

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Modeling using synchrotron absorption in a truncated dipole

Breton et al. 2008

Modeling using synchrotron absorption in a truncated dipole



It works!

Empirical evidence of dipolar magnetic field geometry. Eclipses are a proxy to infer the orientation of pulsar B.



General relativity passes the test once again!

Quantitative measurement of relativistic spin precession.

$$\Omega_{\rm B} = \frac{1}{2} \left(\frac{2\pi}{P_{\rm orb}} \right)^{5/3} \frac{m_{\rm A}(4m_{\rm B} + 3m_{\rm A})}{(1 - e^2)(m_{\rm B} + m_{\rm A})^{4/3}} T_{\odot}^{2/3}$$



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GR predicts: 5:07 yr⁻¹
Measurement: 4:77^{+0;66}/_{-0;65} yr⁻¹

By the way...

Pulsar B disappeared in 2009... so no more "Double Pulsar"

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Testing Theories of Gravity

Strong-field regime

Why are tests of gravity involving pulsars interesting?

"Strong-field" regime:

- Still > 250 000 R_{Schwarzchild} in separation but...
- $E_{binding} \sim 15\% E_{tot}$



Theory-Independent Test of Gravity

Unique test... for a unique double pulsar...

Generalized precession rate is (Damour & Taylor, 1992, Phys. Rev. D):

$$\Omega_{\rm B} = \frac{\sigma_B L}{a_R^3 (1 - e^2)^{3/2}}$$

In terms of a very particular choice of observable timing parameters:

$$arOmega_{
m B}=rac{x_A x_B}{s^2}rac{n^3}{1-e^2}rac{c^2\sigma_B}{\mathcal{G}}$$

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In terms of a very particular choice of observable timing parameters:



The Double Pulsar is the only double neutron star system in which both semimajor axes can be measured independently!

The pulsar-white dwarf binary PSR J1738+0333

See Freire et al. (2012) & Antoniadis et al. (2012)

White dwarf mass from photometry + spectroscopy



Freire et al. (2012) & Antoniadis et al. (2012)

Constraining dipolar gravitational waves



Constraining dipolar gravitational waves



Neutron star + white dwarf binaries have very **different self-gravity**

 $s_{\rm psr} \neq s_{\rm comp}$

Constraining dipolar gravitational waves

 \dot{P}^{D}_{b} and $\dot{P}^{\dot{G}}_{b}$ are degenerate

Combining data from PSRs J1738+0333 and J0437-4715 breaks the degeneracy



Freire et al. (2012) and, also, Lazaridis et al. (2009)

Constraining tensor-scalar theories

A general tensor scalar field $\ln A(\varphi) - \ln A(\varphi_0) = \alpha_0(\varphi - \varphi_0) + \frac{1}{2}\beta_0(\varphi - \varphi_0)^2$

Associated metric $\tilde{g}_{\mu\nu} \equiv A^2(\varphi)g_{\mu\nu}$



Modify the behavior of gravitational constant

 $\tilde{G}_{AB} \equiv G_* A^2(\varphi_0) \cdot (1 + \alpha_A \alpha_B)$

And the Eddington's PPN parameters

$$\gamma_{AB} \equiv 1 - 2 \frac{\alpha_A \alpha_B}{1 + \alpha_A \alpha_B}$$

$$\beta_{BC}^{A} \equiv 1 + \frac{1}{2} \frac{\beta_A \alpha_B \alpha_C}{(1 + \alpha_A \alpha_B)(1 + \alpha_A \alpha_C)}$$

Constraining modified newtonian dynamics

MOND is the non-relativistic limit of tensor-vector-scalar (TeVeS) theories

Associated metric $\tilde{g}_{00} = A^2(\varphi)g_{00}$ and $\tilde{g}_{ij} = A^{-2}(\varphi)g_{ij}$



Modify the behavior of gravitational constant

 $\tilde{G}_{AB} = G_*(1 + \alpha_A \alpha_B)$

And the Eddington's PPN parameters

$$\gamma_{AB} = \gamma^{\text{PPN}} = 1$$

$$\beta_{BC}^{A} \equiv 1 + \frac{1}{2} \frac{\beta_A \alpha_B \alpha_C}{(1 + \alpha_A \alpha_B)(1 + \alpha_A \alpha_C)}$$

More Tests of Gravity?

SEP violation, preferred-frame effects

Pulsar + WD in low eccentricity wide orbit

Test strong equivalence principle $P_{\rm orb}^2/e^2$ $|\Delta| < 4.6 \times 10^{-3}$ Test violation of momentum conservation and preferred frame-effects

statistical: see, e.g., Gonzalez et al. 2011, Stairs et al. 2005 individual system: see, e.g., Wex & Kramer 2007 $P_{\mathrm{orb}}^2/(eP)$ $P_{\mathrm{orb}}^{1/3}/e$

 $|\hat{\alpha}_3| < 5.5 \times 10^{-20}$

Neutron Star Equation-of-State

Probing the upper mass limit of neutron stars



The Future Is Bright

More pulsars, more photons

More pulsars: What if we know "all" pulsars from the Galaxy? More binaries = many new oddballs Not clear how this translates for gravity tests

More photons:

Accurate parallax for large number of pulsars Improved timing on existing systems

Conclusions

